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1. Let  $R = \{(1, 3), (4, 2), (2, 4), (2, 3), (3, 1)\}$  be a relation on the set  $A = \{1, 2, 3, 4\}$ . The relation  $R$  is  
(1) a function (2) reflexive  
(3) not symmetric (4) transitive
2. The range of the function  $f(x) = {}^{7-x}P_{x-3}$  is  
(1)  $\{1, 2, 3\}$  (2)  $\{1, 2, 3, 4, 5\}$   
(3)  $\{1, 2, 3, 4\}$  (4)  $\{1, 2, 3, 4, 5, 6\}$
3. Let  $z, w$  be complex numbers such that  $\bar{z} + i\bar{w} = 0$  and  $\arg zw = \pi$ . Then  $\arg z$  equals  
(1)  $\frac{\pi}{4}$  (2)  $\frac{5\pi}{4}$   
(3)  $\frac{3\pi}{4}$  (4)  $\frac{\pi}{2}$
4. If  $z = x - iy$  and  $z^{\frac{1}{3}} = p + iq$ , then  $\frac{\left(\frac{x}{p} + \frac{y}{q}\right)}{(p^2 + q^2)}$  is equal to  
(1) 1 (2) -2  
(3) 2 (4) -1
5. If  $|z^2 - 1| = |z|^2 + 1$ , then  $z$  lies on  
(1) the real axis (2) an ellipse  
(3) a circle (4) the imaginary axis.
6. Let  $A = \begin{pmatrix} 0 & 0 & -1 \\ 0 & -1 & 0 \\ -1 & 0 & 0 \end{pmatrix}$ . The only correct statement about the matrix  $A$  is  
(1)  $A$  is a zero matrix (2)  $A^2 = I$   
(3)  $A^{-1}$  does not exist (4)  $A = (-1)I$ , where  $I$  is a unit matrix
7. Let  $A = \begin{pmatrix} 1 & -1 & 1 \\ 2 & 1 & -3 \\ 1 & 1 & 1 \end{pmatrix}$  (10)  $B = \begin{pmatrix} 4 & 2 & 2 \\ -5 & 0 & \alpha \\ 1 & -2 & 3 \end{pmatrix}$ . If  $B$  is the inverse of matrix  $A$ , then  $\alpha$  is  
(1) -2 (2) 5  
(3) 2 (4) -1

8. If  $a_1, a_2, a_3, \dots, a_n, \dots$  are in G.P., then the value of the determinant
- $$\begin{vmatrix} \log a_n & \log a_{n+1} & \log a_{n+2} \\ \log a_{n+3} & \log a_{n+4} & \log a_{n+5} \\ \log a_{n+6} & \log a_{n+7} & \log a_{n+8} \end{vmatrix},$$
- is
- (1) 0 (2) -2  
(3) 2 (4) 1
9. Let two numbers have arithmetic mean 9 and geometric mean 4. Then these numbers are the roots of the quadratic equation
- (1)  $x^2 + 18x + 16 = 0$  (2)  $x^2 - 18x - 16 = 0$   
(3)  $x^2 + 18x - 16 = 0$  (4)  $x^2 - 18x + 16 = 0$
10. If  $(1 - p)$  is a root of quadratic equation  $x^2 + px + (1 - p) = 0$ , then its roots are
- (1) 0, 1 (2) -1, 2  
(3) 0, -1 (4) -1, 1
11. Let  $S(K) = 1 + 3 + 5 + \dots + (2K - 1) = 3 + K^2$ . Then which of the following is true?
- (1)  $S(1)$  is correct  
(2) Principle of mathematical induction can be used to prove the formula  
(3)  $S(K) \neq S(K + 1)$   
(4)  $S(K) \Rightarrow S(K + 1)$
12. How many ways are there to arrange the letters in the word GARDEN with the vowels in alphabetical order?
- (1) 120 (2) 480  
(3) 360 (4) 240
13. The number of ways of distributing 8 identical balls in 3 distinct boxes so that none of the boxes is empty is
- (1) 5 (2)  ${}^8C_3$   
(3)  $3^8$  (4) 21
14. If one root of the equation  $x^2 + px + 12 = 0$  is 4, while the equation  $x^2 + px + q = 0$  has equal roots, then the value of 'q' is
- (1)  $\frac{49}{4}$  (2) 4  
(3) 3 (4) 12
15. The coefficient of the middle term in the binomial expansion in powers of x of  $(1 + \alpha x)^4$  and of  $(1 - \alpha x)^6$  is the same if  $\alpha$  equals
- (1)  $-\frac{5}{3}$  (2)  $\frac{3}{5}$   
(3)  $\frac{-3}{10}$  (4)  $\frac{10}{3}$
-

16. The coefficient of  $x^n$  in expansion of  $(1+x)(1-x)^n$  is
- (1)  $(n-1)$  (2)  $(-1)^n(1-n)$   
(3)  $(-1)^{n-1}(n-1)^2$  (4)  $(-1)^{n-1}n$
17. If  $S_n = \sum_{r=0}^n \frac{1}{{}^nC_r}$  and  $t_n = \sum_{r=0}^n \frac{r}{{}^nC_r}$ , then  $\frac{t_n}{S_n}$  is equal to
- (1)  $\frac{1}{2}n$  (2)  $\frac{1}{2}n-1$   
(3)  $n-1$  (4)  $\frac{2n-1}{2}$
18. Let  $T_r$  be the  $r$ th term of an A.P. whose first term is  $a$  and common difference is  $d$ . If for some positive integers  $m, n, m \neq n, T_m = \frac{1}{n}$  and  $T_n = \frac{1}{m}$ , then  $a-d$  equals
- (1) 0 (2) 1  
(3)  $\frac{1}{mn}$  (4)  $\frac{1}{m} + \frac{1}{n}$
19. The sum of the first  $n$  terms of the series  $1^2 + 2 \cdot 2^2 + 3^2 + 2 \cdot 4^2 + 5^2 + 2 \cdot 6^2 + \dots$  is  $\frac{n(n+1)^2}{2}$  when  $n$  is even. When  $n$  is odd the sum is
- (1)  $\frac{3n(n+1)}{2}$  (2)  $\frac{n^2(n+1)}{2}$   
(3)  $\frac{n(n+1)^2}{4}$  (4)  $\left[\frac{n(n+1)}{2}\right]^2$
20. The sum of series  $\frac{1}{2!} + \frac{1}{4!} + \frac{1}{6!} + \dots$  is
- (1)  $\frac{(e^2-1)}{2}$  (2)  $\frac{(e-1)^2}{2e}$   
(3)  $\frac{(e^2-1)}{2e}$  (4)  $\frac{(e^2-2)}{e}$
21. Let  $\alpha, \beta$  be such that  $\pi < \alpha - \beta < 3\pi$ . If  $\sin\alpha + \sin\beta = -\frac{21}{65}$  and  $\cos\alpha + \cos\beta = -\frac{27}{65}$ , then the value of  $\cos\frac{\alpha-\beta}{2}$  is
- (1)  $-\frac{3}{\sqrt{130}}$  (2)  $\frac{3}{\sqrt{130}}$   
(3)  $\frac{6}{65}$  (4)  $-\frac{6}{65}$
-

22. If  $u = \sqrt{a^2 \cos^2 \theta + b^2 \sin^2 \theta} + \sqrt{a^2 \sin^2 \theta + b^2 \cos^2 \theta}$ , then the difference between the maximum and minimum values of  $u^2$  is given by
- (1)  $2(a^2 + b^2)$  (2)  $2\sqrt{a^2 + b^2}$   
 (3)  $(a + b)^2$  (4)  $(a - b)^2$
23. The sides of a triangle are  $\sin \alpha$ ,  $\cos \alpha$  and  $\sqrt{1 + \sin \alpha \cos \alpha}$  for some  $0 < \alpha < \frac{\pi}{2}$ . Then the greatest angle of the triangle is
- (1)  $60^\circ$  (2)  $90^\circ$   
 (3)  $120^\circ$  (4)  $150^\circ$
24. A person standing on the bank of a river observes that the angle of elevation of the top of a tree on the opposite bank of the river is  $60^\circ$  and when he retires 40 meter away from the tree the angle of elevation becomes  $30^\circ$ . The breadth of the river is
- (1) 20 m (2) 30 m  
 (3) 40 m (4) 60 m
25. If  $f : \mathbb{R} \rightarrow \mathbb{S}$ , defined by  $f(x) = \sin x - \sqrt{3} \cos x + 1$ , is onto, then the interval of  $\mathbb{S}$  is
- (1)  $[0, 3]$  (2)  $[-1, 1]$   
 (3)  $[0, 1]$  (4)  $[-1, 3]$
26. The graph of the function  $y = f(x)$  is symmetrical about the line  $x = 2$ , then
- (1)  $f(x + 2) = f(x - 2)$  (2)  $f(2 + x) = f(2 - x)$   
 (3)  $f(x) = f(-x)$  (4)  $f(x) = -f(-x)$
27. The domain of the function  $f(x) = \frac{\sin^{-1}(x - 3)}{\sqrt{9 - x^2}}$  is
- (1)  $[2, 3]$  (2)  $[2, 3)$   
 (3)  $[1, 2]$  (4)  $[1, 2)$
28. If  $\lim_{x \rightarrow \infty} \left(1 + \frac{a}{x} + \frac{b}{x^2}\right)^{2x} = e^2$ , then the values of  $a$  and  $b$ , are
- (1)  $a \in \underline{\underline{\mathbb{R}}}$ ,  $b \in \underline{\underline{\mathbb{R}}}$  (2)  $a = 1$ ,  $b \in \underline{\underline{\mathbb{R}}}$   
 (3)  $a \in \underline{\underline{\mathbb{R}}}$ ,  $b = 2$  (4)  $a = 1$  and  $b = 2$
29. Let  $f(x) = \frac{1 - \tan x}{4x - \pi}$ ,  $x \neq \frac{\pi}{4}$ ,  $x \in \left[0, \frac{\pi}{2}\right]$ . If  $f(x)$  is continuous in  $\left[0, \frac{\pi}{2}\right]$ , then  $f\left(\frac{\pi}{4}\right)$  is
- (1) 1 (2)  $\frac{1}{2}$   
 (3)  $-\frac{1}{2}$  (4) -1
30. If  $x = e^{y + e^{y + \dots \text{to } \infty}}$ ,  $x > 0$ , then  $\frac{dy}{dx}$  is

(1)  $\frac{x}{1+x}$   
(3)  $\frac{1-x}{x}$

(2)  $\frac{1}{x}$   
(4)  $\frac{1+x}{x}$

31. A point on the parabola  $y^2 = 18x$  at which the ordinate increases at twice the rate of the abscissa is

(1) (2, 4) (2) (2, -4)  
(3)  $\left(\frac{-9}{8}, \frac{9}{2}\right)$  (4)  $\left(\frac{9}{8}, \frac{9}{2}\right)$

32. A function  $y = f(x)$  has a second order derivative  $f''(x) = 6(x - 1)$ . If its graph passes through the point (2, 1) and at that point the tangent to the graph is  $y = 3x - 5$ , then the function is

(1)  $(x - 1)^2$  (2)  $(x - 1)^3$   
(3)  $(x + 1)^3$  (4)  $(x + 1)^2$

33. The normal to the curve  $x = a(1 + \cos\theta)$ ,  $y = a\sin\theta$  at ' $\theta$ ' always passes through the fixed point

(1) (a, 0) (2) (0, a)  
(3) (0, 0) (4) (a, a)

34. If  $2a + 3b + 6c = 0$ , then at least one root of the equation  $ax^2 + bx + c = 0$  lies in the interval

(1) (0, 1) (2) (1, 2)  
(3) (2, 3) (4) (1, 3)

35.  $\lim_{n \rightarrow \infty} \sum_{r=1}^n \frac{1}{n} e^{\frac{r}{n}}$  is

(1) e (2) e - 1  
(3) 1 - e (4) e + 1

36. If  $\int \frac{\sin x}{\sin(x - \alpha)} dx = Ax + B \log \sin(x - \alpha) + C$ , then value of (A, B) is

(1)  $(\sin\alpha, \cos\alpha)$  (2)  $(\cos\alpha, \sin\alpha)$   
(3)  $(-\sin\alpha, \cos\alpha)$  (4)  $(-\cos\alpha, \sin\alpha)$

37.  $\int \frac{dx}{\cos x - \sin x}$  is equal to

(1)  $\frac{1}{\sqrt{2}} \log \left| \tan \left( \frac{x}{2} - \frac{\pi}{8} \right) \right| + C$  (2)  $\frac{1}{\sqrt{2}} \log \left| \cot \left( \frac{x}{2} \right) \right| + C$   
(3)  $\frac{1}{\sqrt{2}} \log \left| \tan \left( \frac{x}{2} - \frac{3\pi}{8} \right) \right| + C$  (4)  $\frac{1}{\sqrt{2}} \log \left| \tan \left( \frac{x}{2} + \frac{3\pi}{8} \right) \right| + C$

38. The value of  $\int_{-2}^3 |1 - x^2| dx$  is

(1)  $\frac{28}{3}$

(2)  $\frac{14}{3}$

(3)  $\frac{7}{3}$

(4)  $\frac{1}{3}$

39. The value of  $I = \int_0^{\pi/2} \frac{(\sin x + \cos x)^2}{\sqrt{1 + \sin 2x}} dx$  is

(1) 0

(2) 1

(3) 2

(4) 3

40. If  $\int_0^{\pi} x f(\sin x) dx = A \int_0^{\pi/2} f(\sin x) dx$ , then A is

(1) 0

(2)  $\pi$

(3)  $\frac{\pi}{4}$

(4)  $2\pi$

41. If  $f(x) = \frac{e^x}{1 + e^x}$ ,  $I_1 = \int_{f(-a)}^{f(a)} xg\{x(1-x)\}dx$  and  $I_2 = \int_{f(-a)}^{f(a)} g\{x(1-x)\}dx$  then the value of  $\frac{I_2}{I_1}$  is

(1) 2

(2) -3

(3) -1

(4) 1

42. The area of the region bounded by the curves  $y = |x - 2|$ ,  $x = 1$ ,  $x = 3$  and the x-axis is

(1) 1

(2) 2

(3) 3

(4) 4

43. The differential equation for the family of curves  $x^2 + y^2 - 2ay = 0$ , where a is an arbitrary constant is

(1)  $2(x^2 - y^2)y' = xy$

(2)  $2(x^2 + y^2)y' = xy$

(3)  $(x^2 - y^2)y' = 2xy$

(4)  $(x^2 + y^2)y' = 2xy$

44. The solution of the differential equation  $y dx + (x + x^2y) dy = 0$  is

(1)  $-\frac{1}{xy} = C$

(2)  $-\frac{1}{xy} + \log y = C$

(3)  $\frac{1}{xy} + \log y = C$

(4)  $\log y = Cx$

45. Let A (2, -3) and B(-2, 1) be vertices of a triangle ABC. If the centroid of this triangle moves on the line  $2x + 3y = 1$ , then the locus of the vertex C is the line

(1)  $2x + 3y = 9$

(2)  $2x - 3y = 7$

(3)  $3x + 2y = 5$

(4)  $3x - 2y = 3$

46. The equation of the straight line passing through the point (4, 3) and making intercepts on the co-ordinate axes whose sum is -1 is

(1)  $\frac{x}{2} + \frac{y}{3} = -1$  and  $\frac{x}{-2} + \frac{y}{1} = -1$

(2)  $\frac{x}{2} - \frac{y}{3} = -1$  and  $\frac{x}{-2} + \frac{y}{1} = -1$

$$(3) \frac{x}{2} + \frac{y}{3} = 1 \text{ and } \frac{x}{2} + \frac{y}{1} = 1$$

$$(4) \frac{x}{2} - \frac{y}{3} = 1 \text{ and } \frac{x}{-2} + \frac{y}{1} = 1$$

47. If the sum of the slopes of the lines given by  $x^2 - 2cxy - 7y^2 = 0$  is four times their product, then  $c$  has the value

(1) 1

(2) -1

(3) 2

(4) -2

48. If one of the lines given by  $6x^2 - xy + 4cy^2 = 0$  is  $3x + 4y = 0$ , then  $c$  equals

(1) 1

(2) -1

(3) 3

(4) -3

49. If a circle passes through the point  $(a, b)$  and cuts the circle  $x^2 + y^2 = 4$  orthogonally, then the locus of its centre is

(1)  $2ax + 2by + (a^2 + b^2 + 4) = 0$

(2)  $2ax + 2by - (a^2 + b^2 + 4) = 0$

(3)  $2ax - 2by + (a^2 + b^2 + 4) = 0$

(4)  $2ax - 2by - (a^2 + b^2 + 4) = 0$

50. A variable circle passes through the fixed point  $A(p, q)$  and touches  $x$ -axis. The locus of the other end of the diameter through  $A$  is

(1)  $(x - p)^2 = 4qy$

(2)  $(x - q)^2 = 4py$

(3)  $(y - p)^2 = 4qx$

(4)  $(y - q)^2 = 4px$

51. If the lines  $2x + 3y + 1 = 0$  and  $3x - y - 4 = 0$  lie along diameters of a circle of circumference  $10\pi$ , then the equation of the circle is

(1)  $x^2 + y^2 - 2x + 2y - 23 = 0$

(2)  $x^2 + y^2 - 2x - 2y - 23 = 0$

(3)  $x^2 + y^2 + 2x + 2y - 23 = 0$

(4)  $x^2 + y^2 + 2x - 2y - 23 = 0$

52. The intercept on the line  $y = x$  by the circle  $x^2 + y^2 - 2x = 0$  is  $AB$ . Equation of the circle on  $AB$  as a diameter is

(1)  $x^2 + y^2 - x - y = 0$

(2)  $x^2 + y^2 - x + y = 0$

(3)  $x^2 + y^2 + x + y = 0$

(4)  $x^2 + y^2 + x - y = 0$

53. If  $a \neq 0$  and the line  $2bx + 3cy + 4d = 0$  passes through the points of intersection of the parabolas  $y^2 = 4ax$  and  $x^2 = 4ay$ , then

(1)  $d^2 + (2b + 3c)^2 = 0$

(2)  $d^2 + (3b + 2c)^2 = 0$

(3)  $d^2 + (2b - 3c)^2 = 0$

(4)  $d^2 + (3b - 2c)^2 = 0$

54. The eccentricity of an ellipse, with its centre at the origin, is  $\frac{1}{2}$ . If one of the directrices is  $x = 4$ , then the equation of the ellipse is

(1)  $3x^2 + 4y^2 = 1$

(2)  $3x^2 + 4y^2 = 12$

(3)  $4x^2 + 3y^2 = 12$

(4)  $4x^2 + 3y^2 = 1$

55. A line makes the same angle  $\theta$ , with each of the  $x$  and  $z$  axis. If the angle  $\beta$ , which it makes with  $y$ -axis, is such that  $\sin^2 \beta = 3 \sin^2 \theta$ , then  $\cos^2 \theta$  equals
- (1)  $\frac{2}{3}$  (2)  $\frac{1}{5}$   
 (3)  $\frac{3}{5}$  (4)  $\frac{2}{5}$
56. Distance between two parallel planes  $2x + y + 2z = 8$  and  $4x + 2y + 4z + 5 = 0$  is
- (1)  $\frac{3}{2}$  (2)  $\frac{5}{2}$   
 (3)  $\frac{7}{2}$  (4)  $\frac{9}{2}$
57. A line with direction cosines proportional to 2, 1, 2 meets each of the lines  $x = y + a = z$  and  $x + a = 2y = 2z$ . The co-ordinates of each of the point of intersection are given by
- (1)  $(3a, 3a, 3a)$ ,  $(a, a, a)$  (2)  $(3a, 2a, 3a)$ ,  $(a, a, a)$   
 (3)  $(3a, 2a, 3a)$ ,  $(a, a, 2a)$  (4)  $(2a, 3a, 3a)$ ,  $(2a, a, a)$
58. If the straight lines  $x = 1 + s$ ,  $y = -3 - \lambda s$ ,  $z = 1 + \lambda s$  and  $x = \frac{t}{2}$ ,  $y = 1 + t$ ,  $z = 2 - t$  with parameters  $s$  and  $t$  respectively, are co-planar then  $\lambda$  equals
- (1)  $-2$  (2)  $-1$   
 (3)  $-\frac{1}{2}$  (4)  $0$
59. The intersection of the spheres  $x^2 + y^2 + z^2 + 7x - 2y - z = 13$  and  $x^2 + y^2 + z^2 - 3x + 3y + 4z = 8$  is the same as the intersection of one of the sphere and the plane
- (1)  $x - y - z = 1$  (2)  $x - 2y - z = 1$   
 (3)  $x - y - 2z = 1$  (4)  $2x - y - z = 1$
60. Let  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  be three non-zero vectors such that no two of these are collinear. If the vector  $\vec{a} + 2\vec{b}$  is collinear with  $\vec{c}$  and  $\vec{b} + 3\vec{c}$  is collinear with  $\vec{a}$  ( $\lambda$  being some non-zero scalar) then  $\vec{a} + 2\vec{b} + 6\vec{c}$  equals
- (1)  $\lambda\vec{a}$  (2)  $\lambda\vec{b}$   
 (3)  $\lambda\vec{c}$  (4)  $0$
61. A particle is acted upon by constant forces  $4\hat{i} + \hat{j} - 3\hat{k}$  and  $3\hat{i} + \hat{j} - \hat{k}$  which displace it from a point  $\hat{i} + 2\hat{j} + 3\hat{k}$  to the point  $5\hat{i} + 4\hat{j} + \hat{k}$ . The work done in standard units by the forces is given by
- (1) 40 (2) 30  
 (3) 25 (4) 15
62. If  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  are non-coplanar vectors and  $\lambda$  is a real number, then the vectors  $\vec{a} + 2\vec{b} + 3\vec{c}$ ,  $\lambda\vec{b} + 4\vec{c}$  and  $(2\lambda - 1)\vec{c}$  are non-coplanar for
- (1) all values of  $\lambda$  (2) all except one value of  $\lambda$
-

(3) all except two values of  $\lambda$  (4) no value of  $\lambda$

63. Let  $\bar{u}$ ,  $\bar{v}$ ,  $\bar{w}$  be such that  $|\bar{u}| = 1$ ,  $|\bar{v}| = 2$ ,  $|\bar{w}| = 3$ . If the projection  $\bar{v}$  along  $\bar{u}$  is equal to that of  $\bar{w}$  along  $\bar{u}$  and  $\bar{v}$ ,  $\bar{w}$  are perpendicular to each other then  $|\bar{u} - \bar{v} + \bar{w}|$  equals

- (1) 2 (2)  $\sqrt{7}$   
(3)  $\sqrt{14}$  (4) 14

64. Let  $\bar{a}$ ,  $\bar{b}$  and  $\bar{c}$  be non-zero vectors such that  $(\bar{a} \times \bar{b}) \times \bar{c} = \frac{1}{3} |\bar{b}| |\bar{c}| \bar{a}$ . If  $\theta$  is the acute angle between the vectors  $\bar{b}$  and  $\bar{c}$ , then  $\sin \theta$  equals

- (1)  $\frac{1}{3}$  (2)  $\frac{\sqrt{2}}{3}$   
(3)  $\frac{2}{3}$  (4)  $\frac{2\sqrt{2}}{3}$

65. Consider the following statements:

- (a) Mode can be computed from histogram  
(b) Median is not independent of change of scale  
(c) Variance is independent of change of origin and scale.

Which of these is/are correct?

- (1) only (a) (2) only (b)  
(3) only (a) and (b) (4) (a), (b) and (c)

66. In a series of  $2n$  observations, half of them equal  $a$  and remaining half equal  $-a$ . If the standard deviation of the observations is 2, then  $|a|$  equals

- (1)  $\frac{1}{n}$  (2)  $\sqrt{2}$   
(3) 2 (4)  $\frac{\sqrt{2}}{n}$

67. The probability that A speaks truth is  $\frac{4}{5}$ , while this probability for B is  $\frac{3}{4}$ . The probability that they contradict each other when asked to speak on a fact is

- (1)  $\frac{3}{20}$  (2)  $\frac{1}{5}$   
(3)  $\frac{7}{20}$  (4)  $\frac{4}{5}$

68. A random variable  $X$  has the probability distribution:

X:	1	2	3	4	5	6	7	8
p(X):	0.15	0.23	0.12	0.10	0.20	0.08	0.07	0.05

For the events  $E = \{X \text{ is a prime number}\}$  and  $F = \{X < 4\}$ , the probability  $P(E \cup F)$  is

- (1) 0.87 (2) 0.77  
(3) 0.35 (4) 0.50

69. The mean and the variance of a binomial distribution are 4 and 2 respectively. Then the probability of 2 successes is

- (1)  $\frac{37}{256}$  (2)  $\frac{219}{256}$   
 (3)  $\frac{128}{256}$  (4)  $\frac{28}{256}$

70. With two forces acting at a point, the maximum effect is obtained when their resultant is 4N. If they act at right angles, then their resultant is 3N. Then the forces are  
 (1)  $(2 + \sqrt{2})\text{N}$  and  $(2 - \sqrt{2})\text{N}$  (2)  $(2 + \sqrt{3})\text{N}$  and  $(2 - \sqrt{3})\text{N}$   
 (3)  $\left(2 + \frac{1}{2}\sqrt{2}\right)\text{N}$  and  $\left(2 - \frac{1}{2}\sqrt{2}\right)\text{N}$  (4)  $\left(2 + \frac{1}{2}\sqrt{3}\right)\text{N}$  and  $\left(2 - \frac{1}{2}\sqrt{3}\right)\text{N}$

71. In a right angle  $\triangle ABC$ ,  $\angle A = 90^\circ$  and sides a, b, c are respectively, 5 cm, 4 cm and 3 cm. If a force  $\vec{F}$  has moments 0, 9 and 16 in N cm. units respectively about vertices A, B and C, then magnitude of  $\vec{F}$  is  
 (1) 3 (2) 4  
 (3) 5 (4) 9

72. Three forces  $\vec{P}$ ,  $\vec{Q}$  and  $\vec{R}$  acting along IA, IB and IC, where I is the incentre of a  $\triangle ABC$ , are in equilibrium. Then  $\vec{P} : \vec{Q} : \vec{R}$  is  
 (1)  $\cos \frac{A}{2} : \cos \frac{B}{2} : \cos \frac{C}{2}$  (2)  $\sin \frac{A}{2} : \sin \frac{B}{2} : \sin \frac{C}{2}$   
 (3)  $\sec \frac{A}{2} : \sec \frac{B}{2} : \sec \frac{C}{2}$  (4)  $\operatorname{cosec} \frac{A}{2} : \operatorname{cosec} \frac{B}{2} : \operatorname{cosec} \frac{C}{2}$

73. A particle moves towards east from a point A to a point B at the rate of 4 km/h and then towards north from B to C at the rate of 5 km/h. If  $AB = 12$  km and  $BC = 5$  km, then its average speed for its journey from A to C and resultant average velocity direct from A to C are respectively  
 (1)  $\frac{17}{4}$  km/h and  $\frac{13}{4}$  km/h (2)  $\frac{13}{4}$  km/h and  $\frac{17}{4}$  km/h  
 (3)  $\frac{17}{9}$  km/h and  $\frac{13}{9}$  km/h (4)  $\frac{13}{9}$  km/h and  $\frac{17}{9}$  km/h

74. A velocity  $\frac{1}{4}$  m/s is resolved into two components along OA and OB making angles  $30^\circ$  and  $45^\circ$  respectively with the given velocity. Then the component along OB is  
 (1)  $\frac{1}{8}$  m/s (2)  $\frac{1}{4}(\sqrt{3} - 1)$  m/s  
 (3)  $\frac{1}{4}$  m/s (4)  $\frac{1}{8}(\sqrt{6} - \sqrt{2})$  m/s

75. If  $t_1$  and  $t_2$  are the times of flight of two particles having the same initial velocity u and range R on the horizontal, then  $t_1^2 + t_2^2$  is equal to  
 (1)  $\frac{u^2}{g}$  (2)  $\frac{4u^2}{g^2}$

$$(3) \frac{u^2}{2g}$$

(4) 1

# FIITJEE AIEEE – 2004 (MATHEMATICS)

## ANSWERS

1. 3	16. 2	31. 4	46. 4	61. 1
2. 1	17. 1	32. 2	47. 3	62. 3
3. 3	18. 1	33. 1	48. 4	63. 3
4. 2	19. 2	34. 1	49. 2	64. 4
5. 4	20. 2	35. 2	50. 1	65. 3
6. 2	21. 1	36. 2	51. 1	66. 3
7. 2	22. 4	37. 4	52. 1	67. 3
8. 1	23. 3	38. 1	53. 1	68. 2
9. 4	24. 1	39. 3	54. 2	69. 4
10. 3	25. 4	40. 2	55. 3	70. 3
11. 4	26. 2	41. 1	56. 3	71. 3
12. 3	27. 2	42. 1	57. 2	72. 1
13. 4	28. 2	43. 3	58. 1	73. 1
14. 1	29. 3	44. 2	59. 4	74. 4
15. 3	30. 3	45. 1	60. 4	75. 2

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